

Given the ordered pairs for the initial and terminal points of each vector, are the two vectors equivalent?

- $$1) \ A(-1, 3), B(4, 5), C(-5, -2), D(0,0)$$

$$\overrightarrow{AB}, \overrightarrow{CD}$$

- A) No

$$\overrightarrow{AB}, \overrightarrow{II}$$



## Solve.

- 3) Two forces of 589 newtons and 246 newtons act at a point. The resultant force is 667 newtons. Find the angle between the forces.

A)  $97.4^\circ$       B)  $164.3^\circ$       C)  $114.3^\circ$       D)  $82.6^\circ$

4) Starting at point A, a ship sails 74 km on a bearing of  $203^\circ$ , then turns and sails 36 km on a bearing of  $293^\circ$ . Find the distance of the ship from point A.

A) 110 km      B) 82 km      C) 8 km      D) 118 km

5) A plane is heading due south with an airspeed of 246 mph. A wind from a direction of  $52^\circ$  is blowing at 8 mph. Find the bearing of the plane.

A)  $89^\circ$       B)  $181^\circ$       C)  $94^\circ$       D)  $176^\circ$

6) A wind has an easterly component of 5 km/h and a northerly component of 16 km/h. Find the direction of the wind.

A)  $54.5^\circ$       B)  $-3.3^\circ$       C)  $72.6^\circ$       D)  $17.4^\circ$

Given the magnitudes of vectors  $u$  and  $v$  and the angle  $\theta$  between them, find the magnitude of the sum  $u + v$  to the nearest tenth and the angle that the sum vector makes with  $u$  to the nearest degree.

- 7)  $|\mathbf{u}| = 55$ ,  $|\mathbf{v}| = 55$ ,  $\theta = 14^\circ$

A) 109.2,  $14^\circ$       B) 110,  $14^\circ$       C) 109.2,  $7^\circ$       D) 110,  $7^\circ$

8)  $|\mathbf{u}| = 85$ ,  $|\mathbf{v}| = 85$ ,  $\theta = 10^\circ$

A) 169.4,  $5^\circ$       B) 170,  $5^\circ$       C) 169.4,  $10^\circ$       D) 170,  $10^\circ$

## Solve.

- 9) What is the minimum force required to prevent a ball weighing 15.1 lb from rolling down a ramp inclined  $23.2^\circ$  with the horizontal?

A) 3 lb      B) 13.9 lb      C) 7 lb      D) 5.9 lb

10) A vector with magnitude of 200 lb is inclined to the left and downward  $51^\circ$  from the horizontal. Resolve the vector into components.

A) Left: 125.9, down: 155.4      B) Left: 257.4, down: 317.8  
C) Left: 317.8, down: 257.4      D) Left: 155.4, down: 125.9

- 11) A luggage wagon is being pulled with vector force  $\mathbf{V}$ , which has a magnitude of 620 lb at an angle of elevation of  $65^\circ$ . Resolve the vector  $\mathbf{V}$  into components.
- A) Horizontal: 262, vertical: 561.9  
 B) Horizontal: 561.9, vertical: 262  
 C) Horizontal: 684.1, vertical: 1467  
 D) Horizontal: 1467, vertical: 684.1

**Find the component form of the vector given the initial and terminal points.**

- 12)  $\overrightarrow{MN}$ ; M(11, 1), N(8, 10)  
 A)  $\langle 9, -3 \rangle$       B)  $\langle -3, 9 \rangle$       C)  $\langle 19, 11 \rangle$       D)  $\langle 3, -9 \rangle$

**Find the length of the vector given the initial and terminal points.**

- 13)  $\overrightarrow{MN}$ ; M(9, 8), N(10, 12)  
 A)  $\sqrt{5}$       B)  $\sqrt{17}$       C) 17      D) 5

**Find the indicated quantity.**

- 14) Find the magnitude of the vector  $\mathbf{u}$  if  $\mathbf{u} = \langle -5, 9 \rangle$ .  
 A)  $\sqrt{106}$       B) 7      C)  $2\sqrt{14}$       D) 106
- 15) Find the magnitude of the vector  $\mathbf{u}$  if  $\mathbf{u} = \langle 2, 4 \rangle$ .  
 A) 3      B)  $2\sqrt{5}$       C) 20      D)  $2\sqrt{3}$

**Perform the indicated operation.**

- 16)  $\mathbf{u} = \langle -7, 3 \rangle$ ,  $\mathbf{v} = \langle -7, 6 \rangle$ ,  $\mathbf{w} = \langle -3, -5 \rangle$   
 $\mathbf{v} - (2\mathbf{w} + 3\mathbf{u})$   
 A)  $\langle -22, 25 \rangle$       B)  $\langle 3, 8 \rangle$       C)  $\langle 20, 8 \rangle$       D)  $\langle 20, 7 \rangle$

**Find the dot product for the given vectors.**

- 17)  $\mathbf{u} = \langle 1, 12 \rangle$ ,  $\mathbf{v} = \langle 11, 5 \rangle$   
 A) 137      B) -49      C) 67      D) 71
- 18)  $\mathbf{u} = \langle 7, -1 \rangle$ ,  $\mathbf{v} = \langle 2, 8 \rangle$   
 A) 54      B) 6      C) 9      D) 22

**Find a unit vector that has the same direction as the given vector.**

- 19)  $\mathbf{v} = \langle 8, 15 \rangle$   
 A)  $\left\langle \frac{8}{17}, \frac{15}{17} \right\rangle$       B)  $\langle 136, 255 \rangle$       C)  $\left\langle \frac{15}{17}, \frac{8}{17} \right\rangle$       D)  $\left\langle \frac{17}{8}, \frac{17}{15} \right\rangle$
- 20)  $\mathbf{w} = \langle -9, 8 \rangle$   
 A)  $\left\langle \frac{-9}{\sqrt{145}}, \frac{8}{\sqrt{145}} \right\rangle$       B)  $\left\langle \frac{8}{\sqrt{145}}, \frac{-9}{\sqrt{145}} \right\rangle$       C)  $\left\langle -\frac{\sqrt{145}}{9}, \frac{\sqrt{145}}{8} \right\rangle$       D)  $\langle -9\sqrt{145}, 8\sqrt{145} \rangle$

**Express the given vector as a linear combination of the unit vectors  $\mathbf{i}$  and  $\mathbf{j}$ .**

- 21)  $\mathbf{w} = \langle -3, 10 \rangle$   
 A)  $3\mathbf{i} - 10\mathbf{j}$       B)  $-3\mathbf{i} - 10\mathbf{j}$       C)  $3\mathbf{i} + 10\mathbf{j}$       D)  $-3\mathbf{i} + 10\mathbf{j}$
- 22)  $\mathbf{u} = \langle 2, 9 \rangle$   
 A)  $9\mathbf{i} + 2\mathbf{j}$       B)  $9\mathbf{i} - 2\mathbf{j}$       C)  $2\mathbf{i} + 9\mathbf{j}$       D)  $2\mathbf{i} - 9\mathbf{j}$

**Perform the indicated operation.**

23)  $\mathbf{u} = 5\mathbf{i} + \mathbf{j}$ ,  $\mathbf{v} = -7\mathbf{i} - 4\mathbf{j}$   
 $6\mathbf{v} - \mathbf{u}$

- A)  $-47\mathbf{i} - 5\mathbf{j}$       B)  $25\mathbf{i} + 47\mathbf{j}$       C)  $-37\mathbf{i} + 25\mathbf{j}$       D)  $-47\mathbf{i} - 25\mathbf{j}$

**Calculate the unit vector  $\mathbf{u} = (\cos \theta)\mathbf{i} + (\sin \theta)\mathbf{j}$  for the given direction angle.**

24)  $\theta = \frac{\pi}{4}$

- A)  $\frac{\sqrt{3}}{2}\mathbf{i} + \frac{1}{2}\mathbf{j}$       B)  $\frac{1}{2}\mathbf{i} + \frac{\sqrt{3}}{2}\mathbf{j}$       C)  $\frac{\sqrt{2}}{2}\mathbf{i} - \frac{\sqrt{2}}{2}\mathbf{j}$       D)  $\frac{\sqrt{2}}{2}\mathbf{i} + \frac{\sqrt{2}}{2}\mathbf{j}$

**Determine the direction angle  $\theta$  of the vector, to the nearest degree.**

25)  $\mathbf{u} = \langle 4, 6 \rangle$

- A)  $56^\circ$       B)  $214^\circ$       C)  $34^\circ$       D)  $236^\circ$

26)  $\mathbf{w} = \langle 1, -8 \rangle$

- A)  $-7^\circ$       B)  $353^\circ$       C)  $277^\circ$       D)  $97^\circ$

**Find the magnitude or direction angle of the given vector as indicated.**

27)  $\mathbf{u} = 7[(\cos 30^\circ)\mathbf{i} + (\sin 30^\circ)\mathbf{j}]$ ; Find the magnitude.

- A) 14      B) 7      C)  $\frac{7}{2}$       D)  $\sqrt{7}$

28)  $\mathbf{w} = \left\langle \frac{\sqrt{3}}{2}, \frac{1}{2} \right\rangle$ ; Find the magnitude.

- A)  $\sqrt{2}$       B) 1      C)  $\frac{1}{2}$       D) 2

**Find the angle between the given vectors, to the nearest tenth of a degree.**

29)  $\mathbf{u} = \langle 3, 2 \rangle$ ,  $\mathbf{v} = \langle 6, 6 \rangle$

- A)  $-11.3^\circ$       B)  $11.3^\circ$       C)  $78.7^\circ$       D)  $101.3^\circ$

30)  $\mathbf{t} = \langle -2, -6 \rangle$ ,  $\mathbf{s} = \langle 1, 2 \rangle$

- A)  $45^\circ$       B)  $8.1^\circ$       C)  $-81.9^\circ$       D)  $171.9^\circ$

31)  $\mathbf{u} = \mathbf{i} - \mathbf{j}$ ,  $\mathbf{v} = 4\mathbf{i} + 5\mathbf{j}$

- A)  $99^\circ$       B)  $96.3^\circ$       C)  $6.3^\circ$       D)  $-6.3^\circ$

**Express the vector as a product of its magnitude and direction.**

32)  $4\mathbf{i} + 3\mathbf{j}$

- A)  $5\left(\frac{4}{5}\mathbf{i} + \frac{3}{5}\mathbf{j}\right)$       B)  $5(20\mathbf{i} + 15\mathbf{j})$       C)  $5\left(\frac{4}{25}\mathbf{i} + \frac{3}{25}\mathbf{j}\right)$       D)  $5\left(\frac{1}{5}\mathbf{i} + \frac{1}{5}\mathbf{j}\right)$

**Solve the problem using the vector form  $\mathbf{v} = |\mathbf{v}| [(\cos \theta)\mathbf{i} + (\sin \theta)\mathbf{j}]$ .**

33) An airplane has an airspeed of 125 km/h. It is to make a flight in a direction of  $305^\circ$  while there is a 30 - km/h wind from  $210^\circ$ . What will the airplane's actual heading be?

- A)  $283^\circ$       B)  $292^\circ$       C)  $318^\circ$       D)  $107^\circ$

## Answer Key

Testname: MATH140STUDYGUIDEII

- 1) B
- 2) A
- 3) D
- 4) B
- 5) B
- 6) C
- 7) C
- 8) A
- 9) D
- 10) A
- 11) A
- 12) B
- 13) B
- 14) A
- 15) B
- 16) D
- 17) D
- 18) B
- 19) A
- 20) A
- 21) D
- 22) C
- 23) D
- 24) D
- 25) A
- 26) C
- 27) B
- 28) B
- 29) B
- 30) D
- 31) B
- 32) A
- 33) C